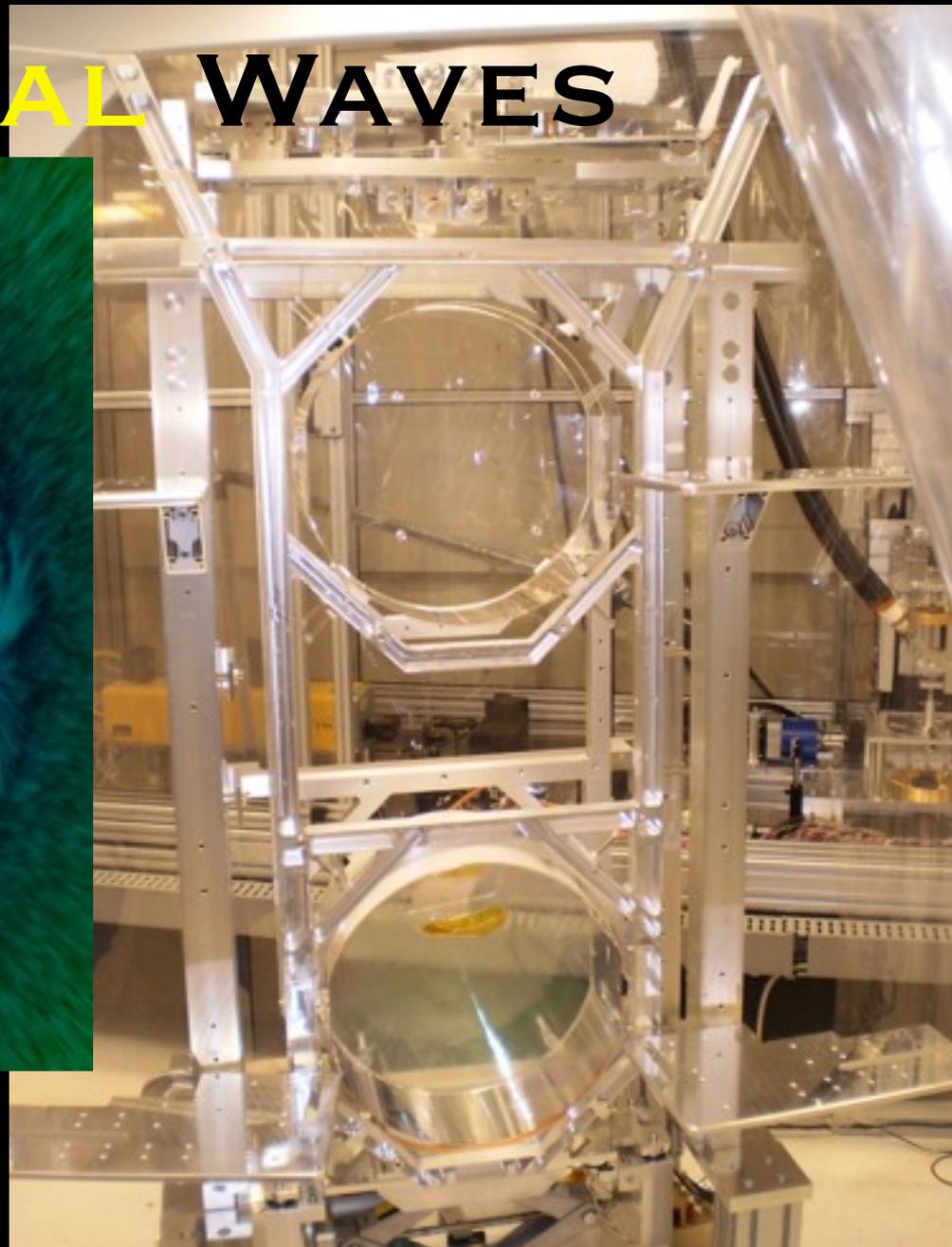
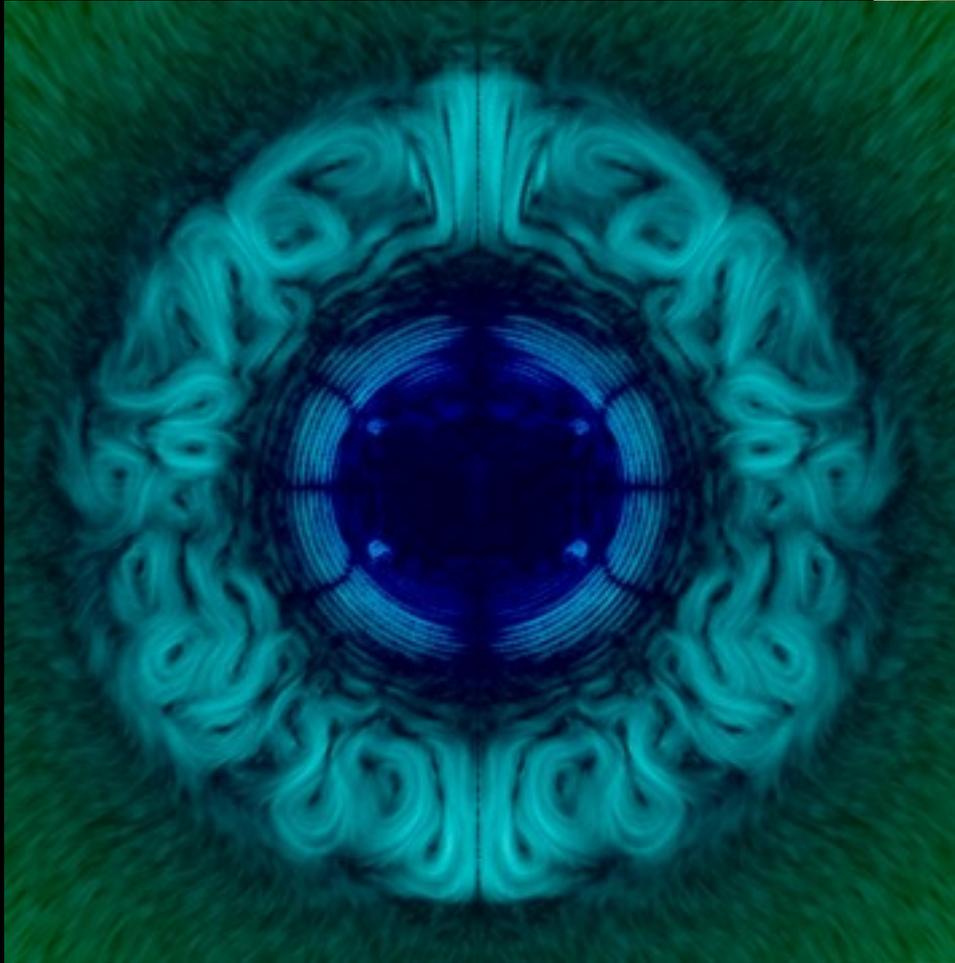


GRAVITATIONAL WAVES



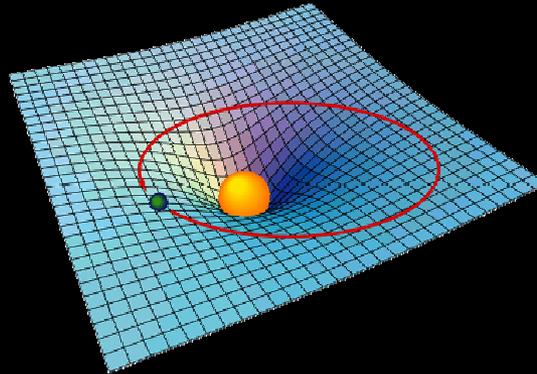
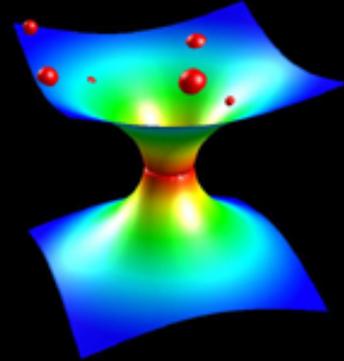
NASA QFT

Jan 18, 2012

Rana Adhikari Caltech

Gravitational Waves

$$G_{\mu\nu} = (8\pi G/c^4)T_{\mu\nu}$$



“Mass tells space-time how to curve,
and space-time tells mass how to move.”
--- John Wheeler

Einstein's Equations:

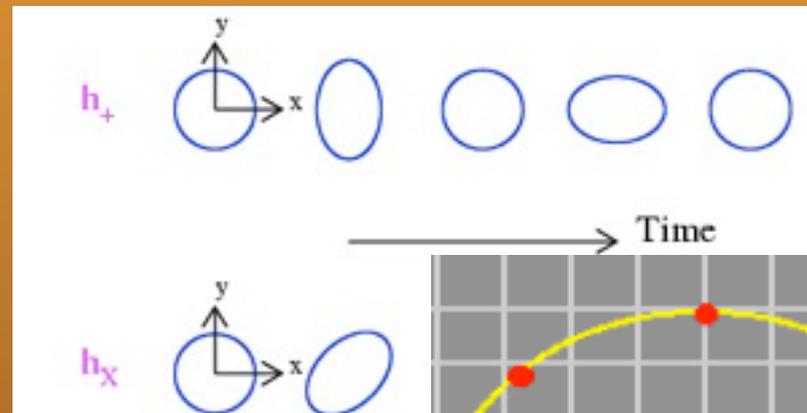
When matter moves, or changes its configuration, its gravitational field changes. This change propagates outward as a *ripple in the curvature of space-time*: a **gravitational wave**.

Gravitational Waves?

- Gravitational Waves = “Ripples in space-time”
- Two transverse polarizations - quadrupolar: + and x

Example:

Ring of test masses
responding to wave
propagating along z

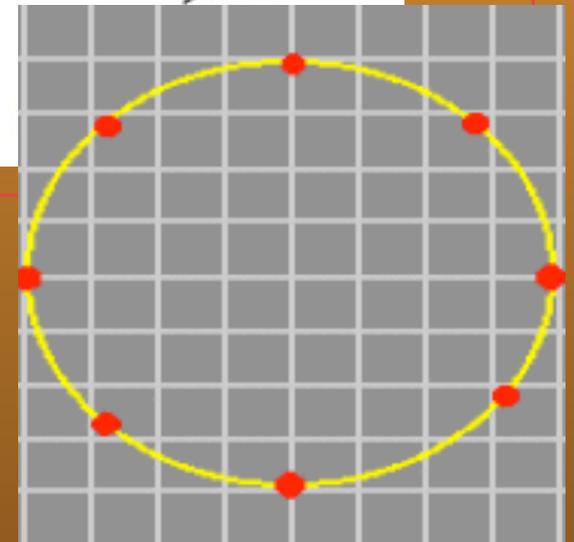


Amplitude parameterized by

dimensionless strain h : $\Delta L \sim h(t) \times L$

Need to measure strain of $\sim 10^{-21}$ - 10^{-22}

We want a very large 'L'



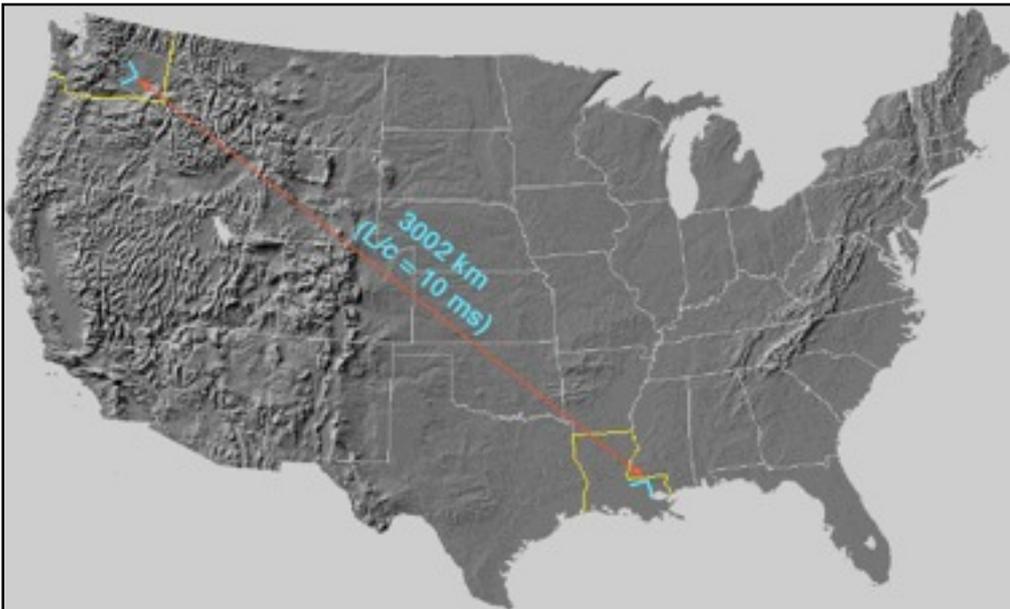
LIGO: Big Michelson Interferometers



Hanford Nuclear Reservation,
Eastern WA (H1 4km, H2 2km)



- *Interferometers are aligned to be as close to parallel to each other as possible*
- *Observing signals in coincidence increases the detection confidence*
- *Determine source location on the sky, propagation speed and polarization of the gravity wave*

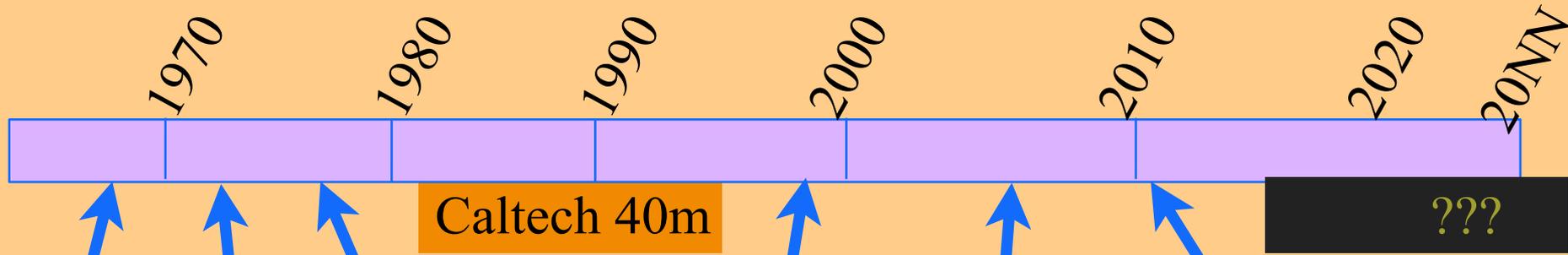


Livingston, LA (L1 4km)

~1 hour from New Orleans



Timeline of GW Detectors



1st Bar Detectors (Weber)

1st Tabletop Interferometer (Forward, Malibu)

Interferometer Concept (Weiss, MIT)

km scale Interferometers (Japan, U.S., Germany, Italy)

km scale Interferometers @ design sensitivity

2nd Gen Interferometers



The Michelson Interferometer

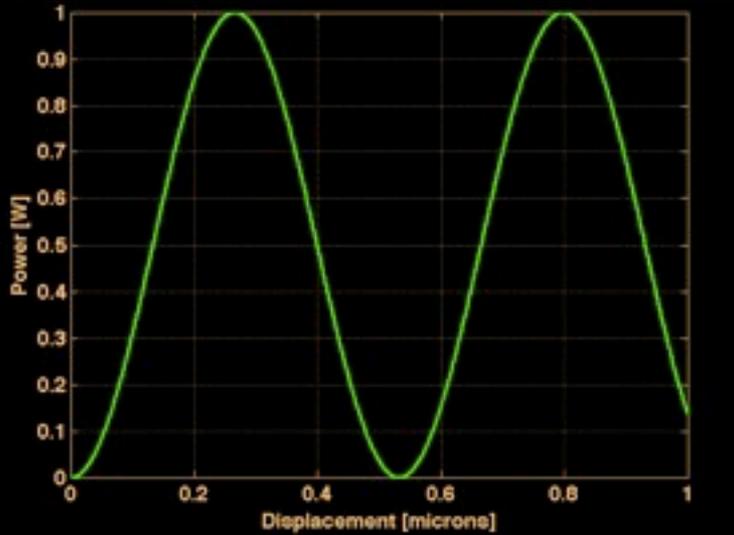
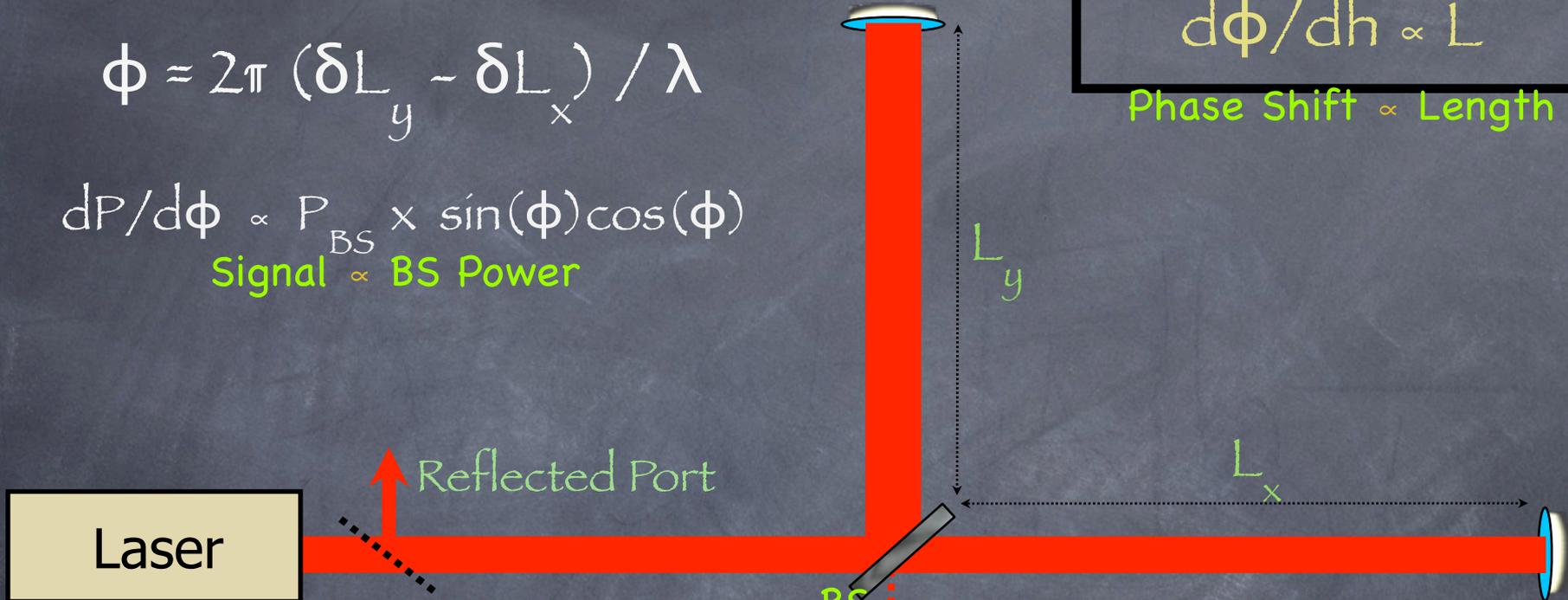
$$\phi = 2\pi (\delta L_y - \delta L_x) / \lambda$$

$$dP/d\phi \propto P_{BS} \times \sin(\phi)\cos(\phi)$$

Signal \propto BS Power

$$d\phi/dh \propto L$$

Phase Shift \propto Length



Anti-Symmetric
(Dark) Port

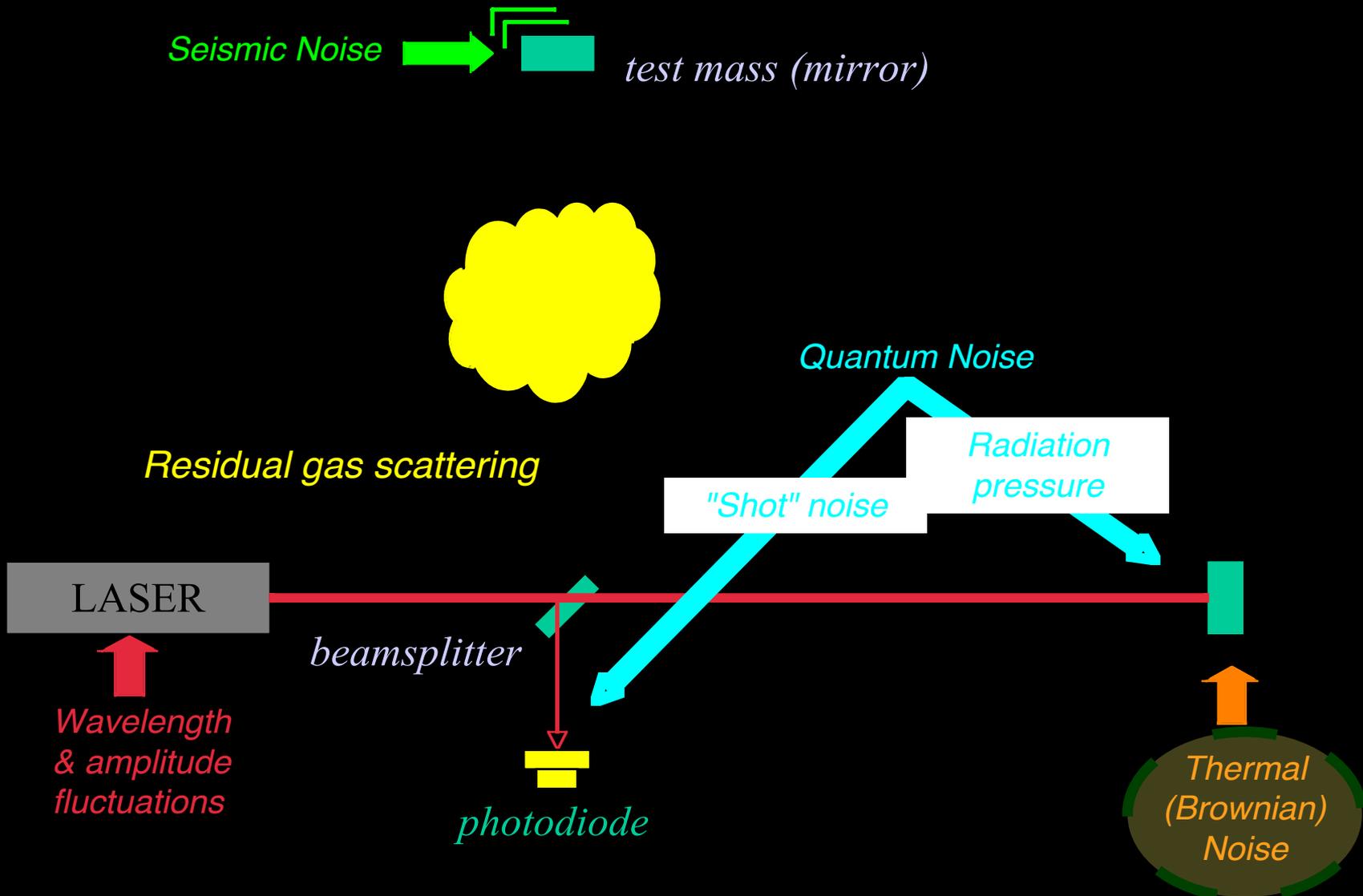
$$P \propto P_{BS} \times \sin^2(\phi)$$

Poisson Statistics...

$$dP \propto \text{sqrt}(P)$$

Shot Noise

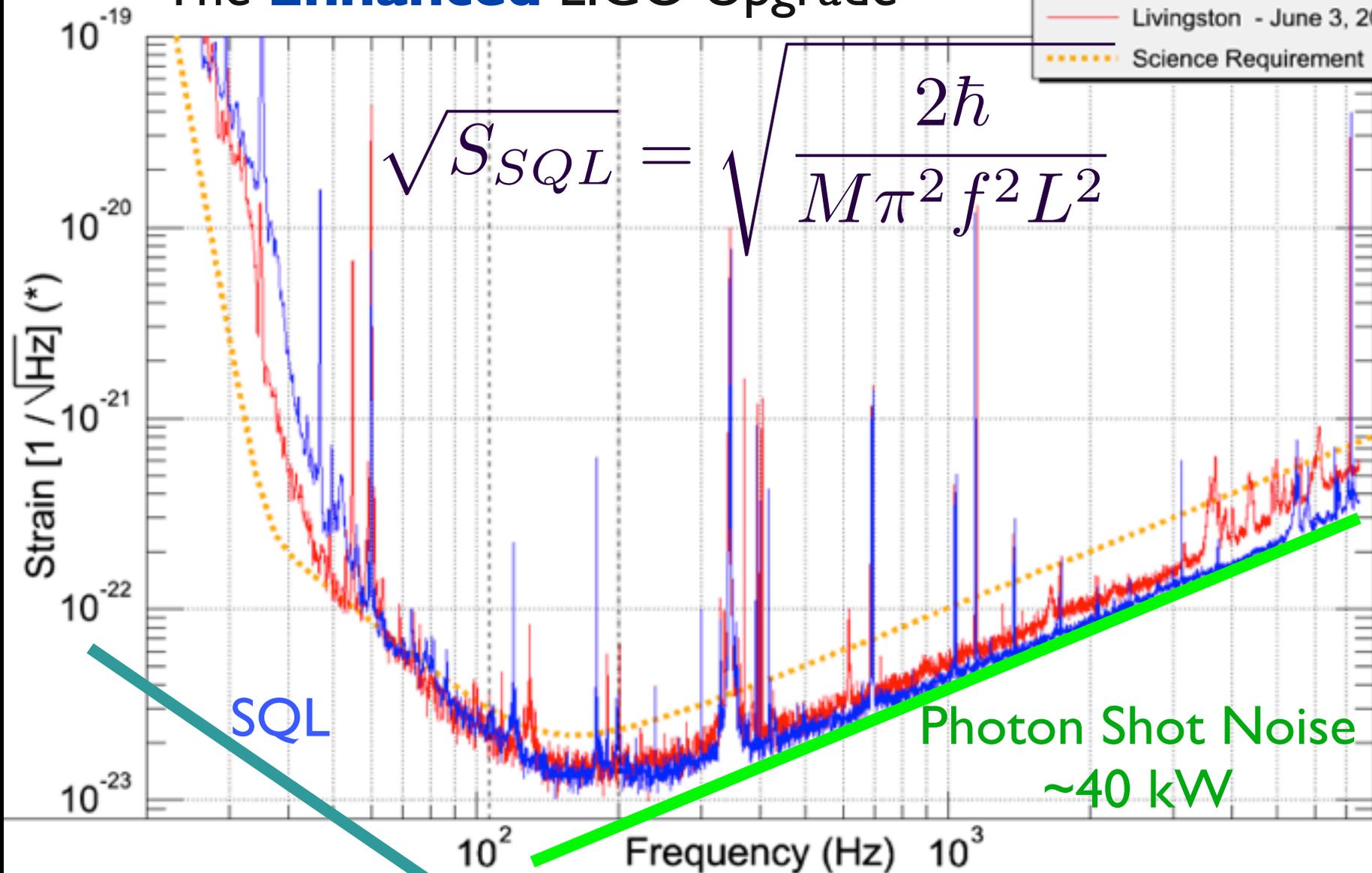
Noise Cartoon



The **Enhanced** LIGO Upgrade

- Hanford - June 2, 2010
- Livingston - June 3, 2010
- ⋯ Science Requirement

$$\sqrt{S_{SQL}} = \sqrt{\frac{2\hbar}{M\pi^2 f^2 L^2}}$$



*T0=02/06/2010 05:35:00

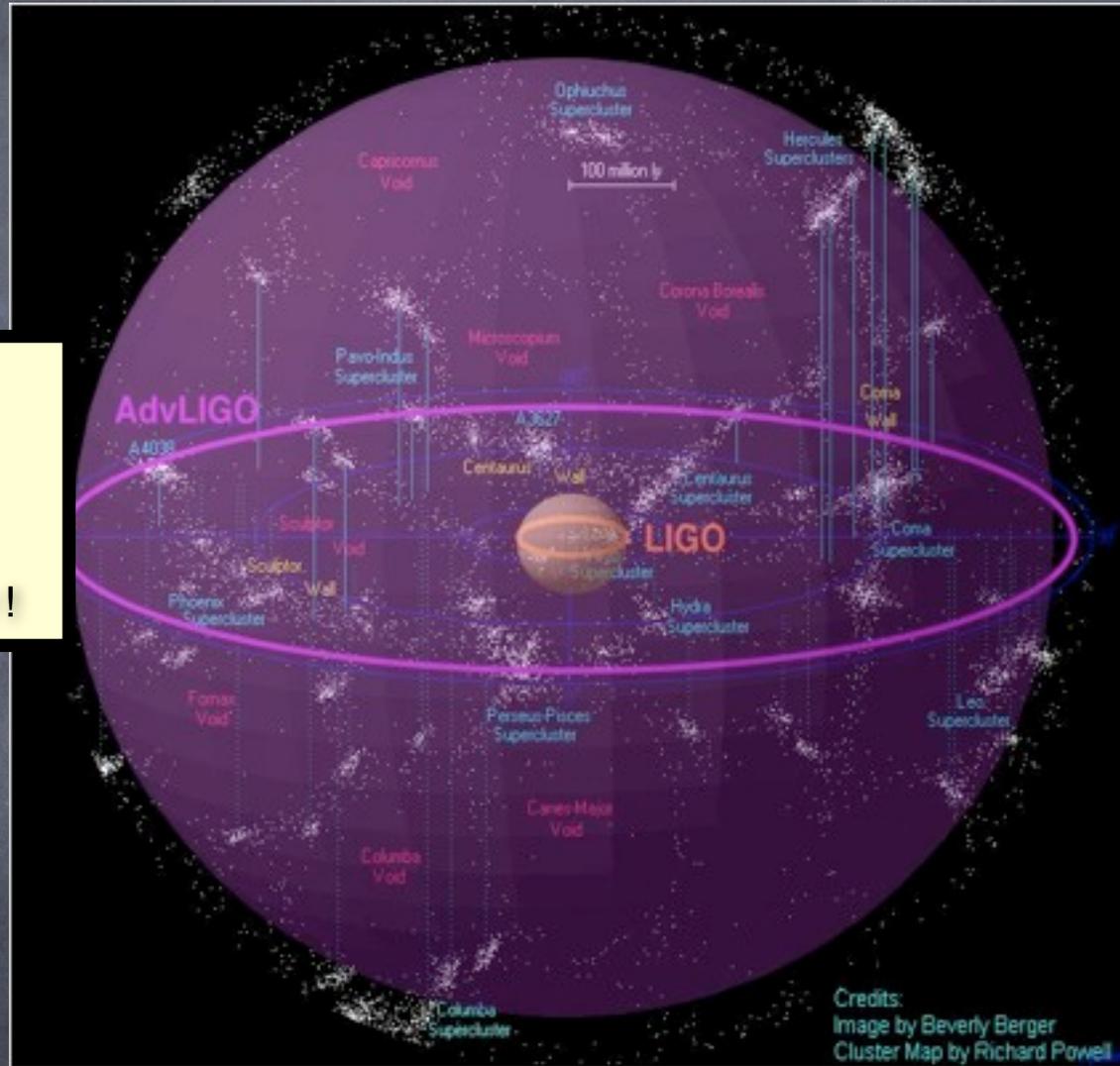
*Avg=25/Bin=5L

*BW=0.187493

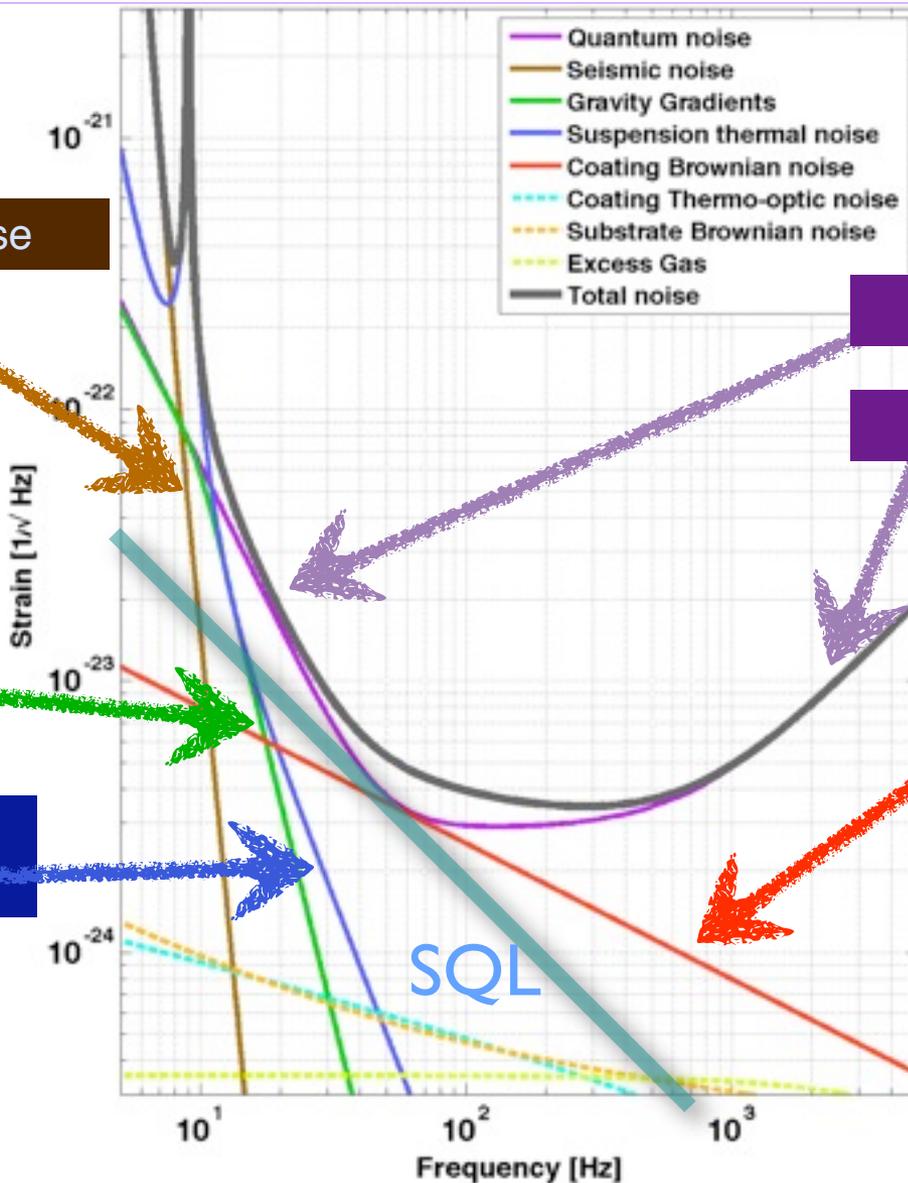


Advanced LIGO

x10 better amplitude sensitivity
⇒ **x1000** rate=(reach)³
⇒ 1 day of Advanced LIGO
» 1 year of Initial LIGO !



Advanced LIGO Noise Breakdown



Filtered Seismic Noise

Seismic / Acoustic Fluctuations
-> Fluctuations in Newtonian Gravity

Mirror Suspension Thermal Noise

Radiation Pressure

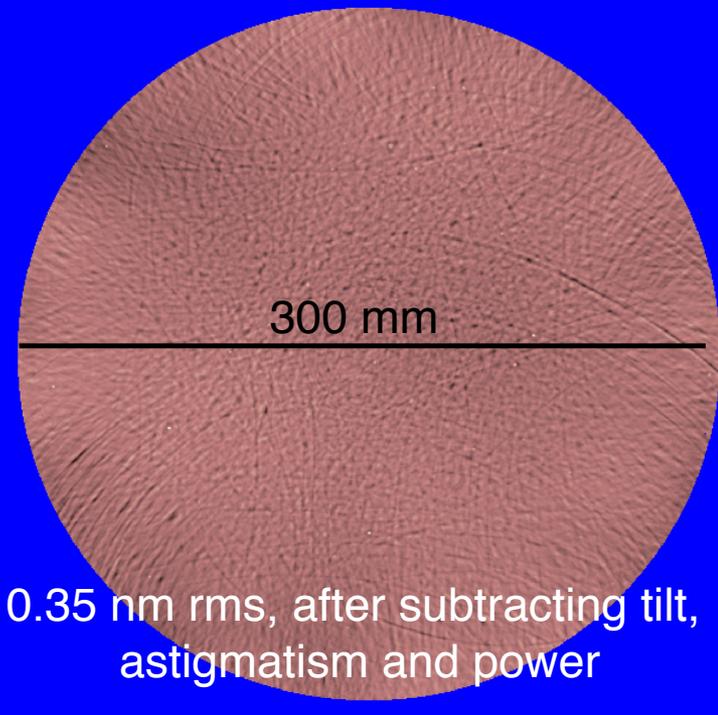
Shot Noise (~1 MW)

Thermal Noise in Mirror Coatings

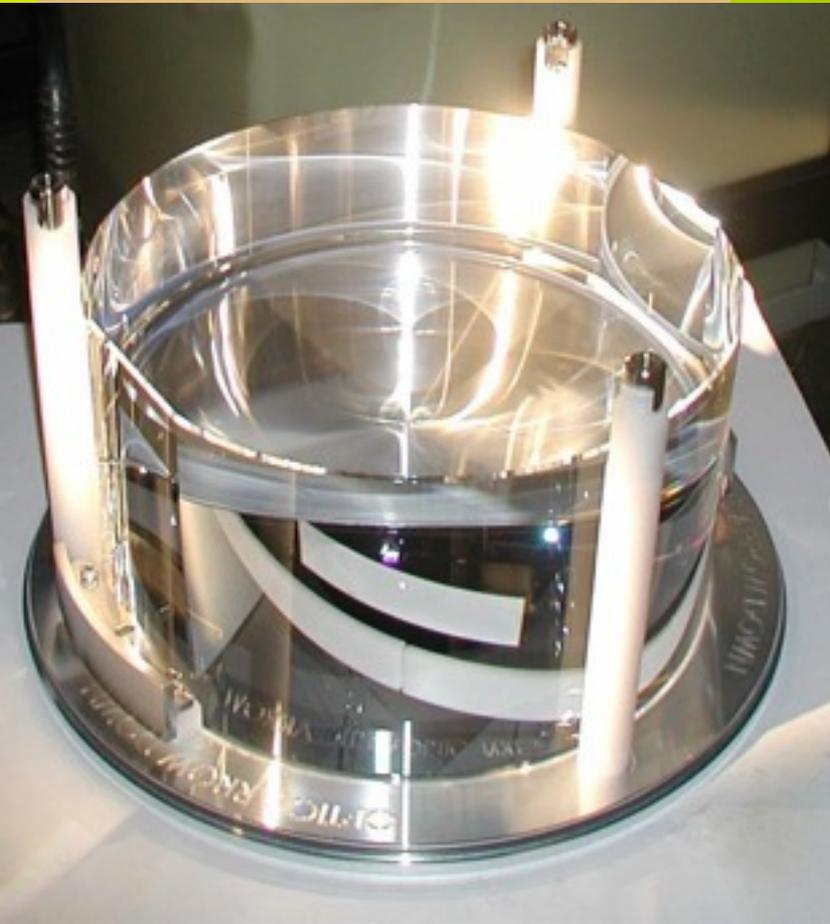
SQL

Large Optics

- Size: 34 cm wide, 20 cm thick => 40 kg
- Material: Heraeus Suprasil Silica
- Bulk Absorption: 0.2 ppm/cm
- Coating absorption: 0.5 ppm/bounce
- High Q (10^8) -> low thermal noise



0.35 nm rms, after subtracting tilt, astigmatism and power



Brownian Thermal Fluctuations

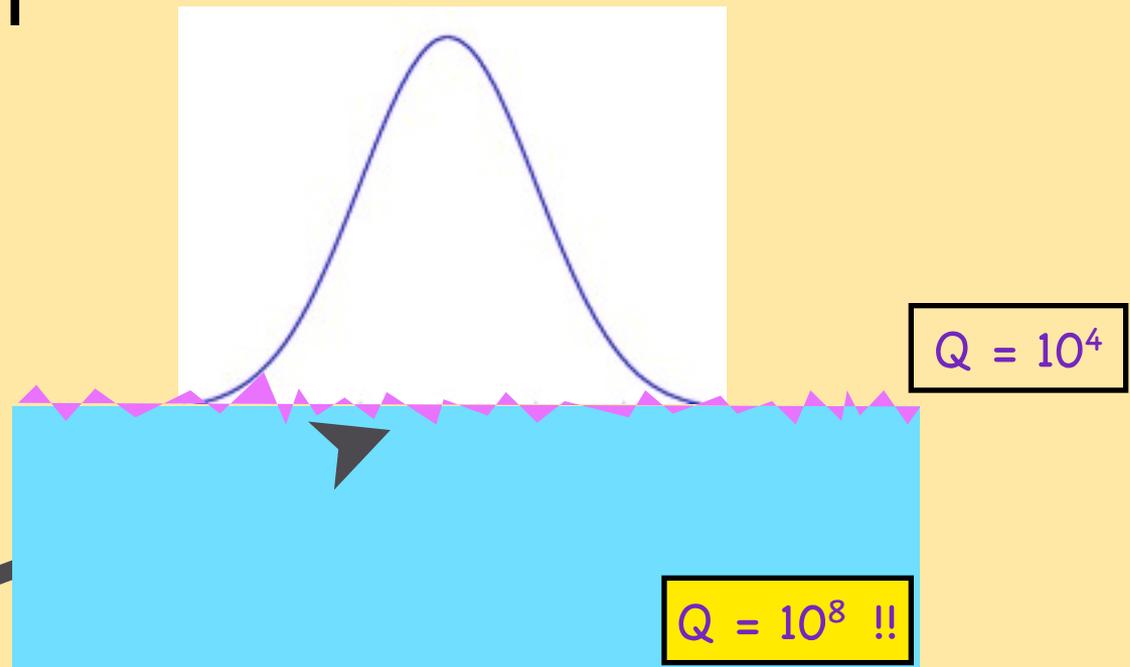
$$S_x(\omega) = \frac{4k_B T}{\omega^2 \text{Re}[Z(\omega)]}$$

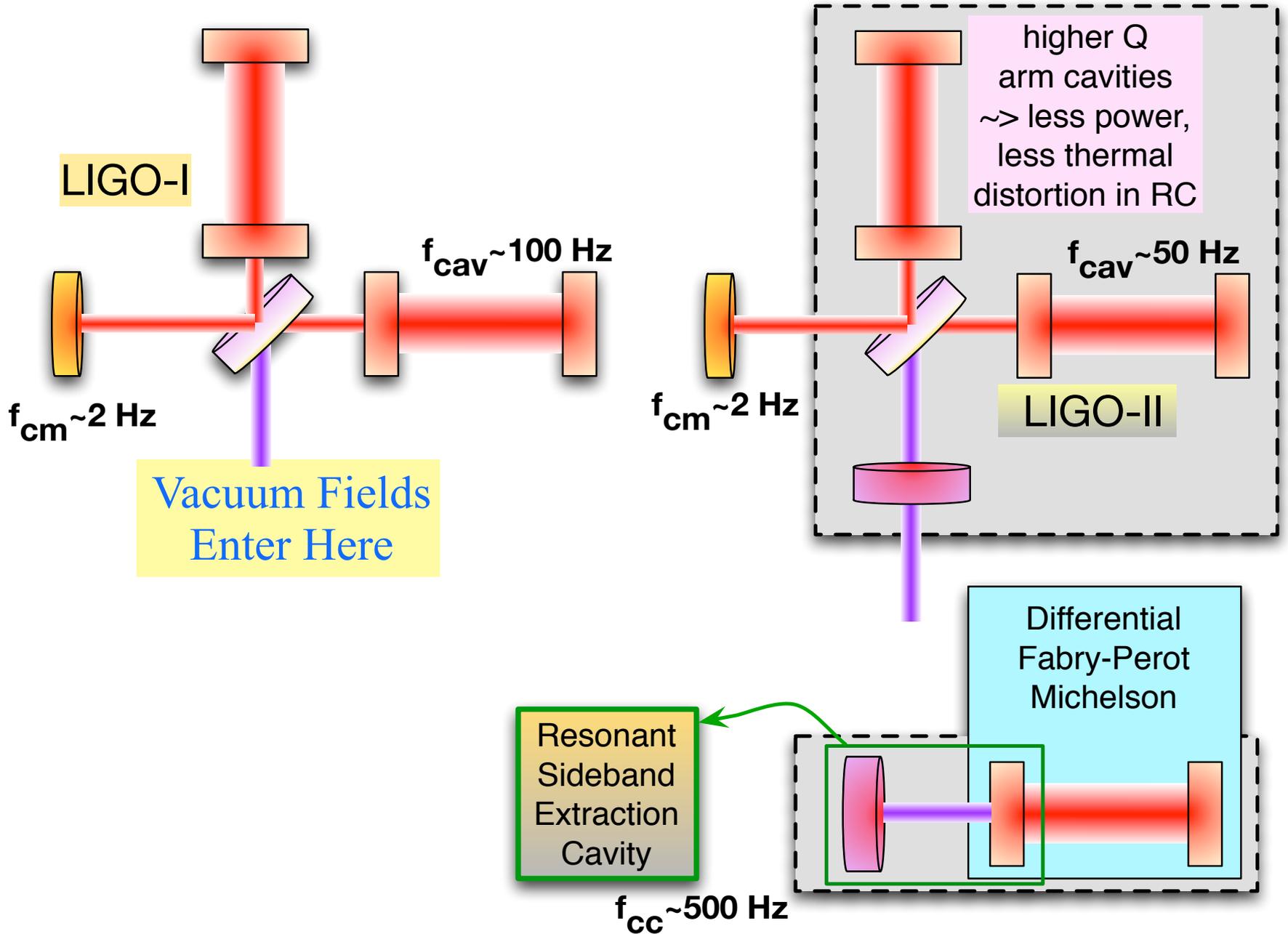
Simple
Harmonic
Oscillator

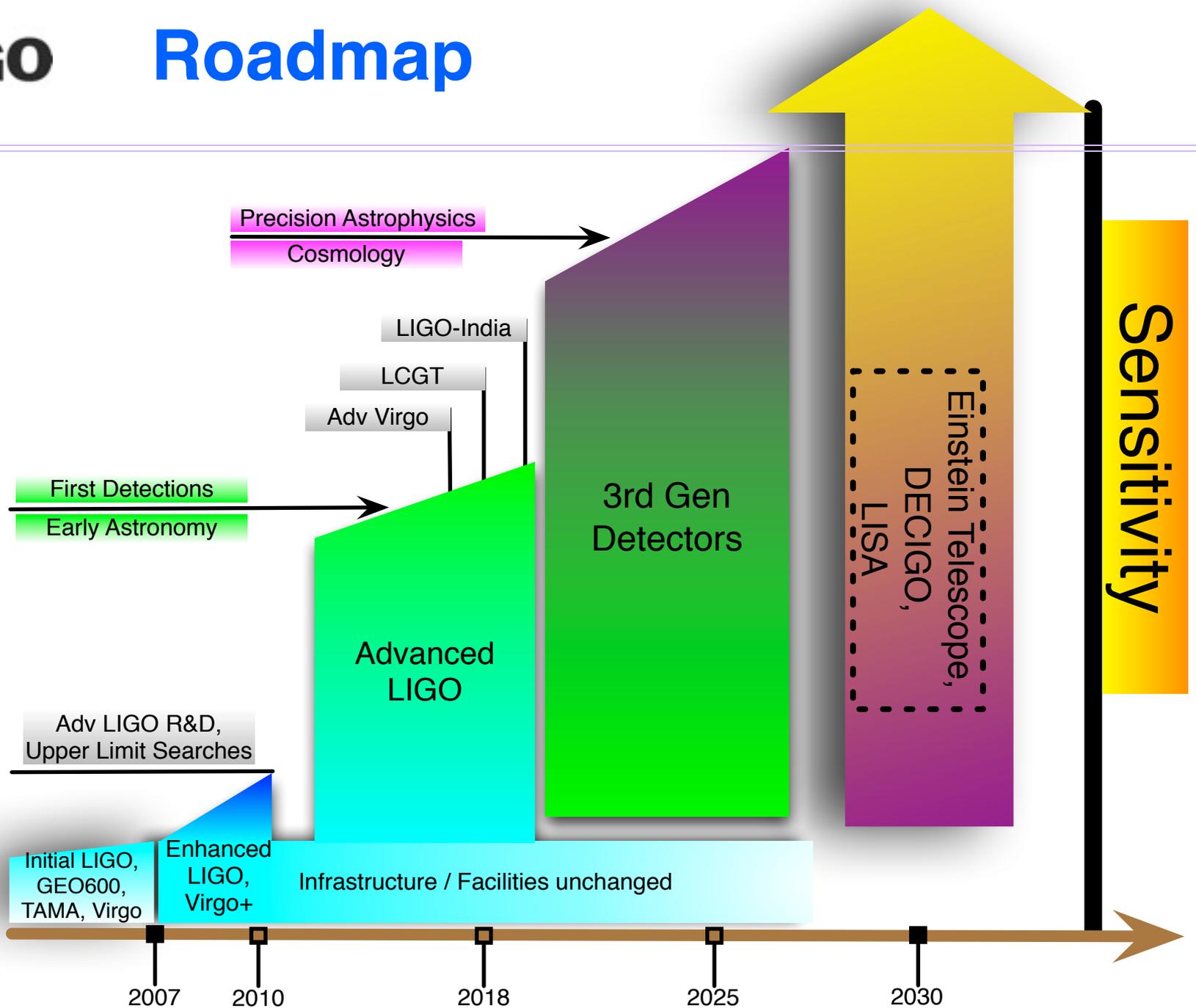
$$Z(\omega) = \frac{\dot{x}}{F} = \frac{K - M\omega^2}{i\omega}$$

Fluctuation
Dissipation
Theorem

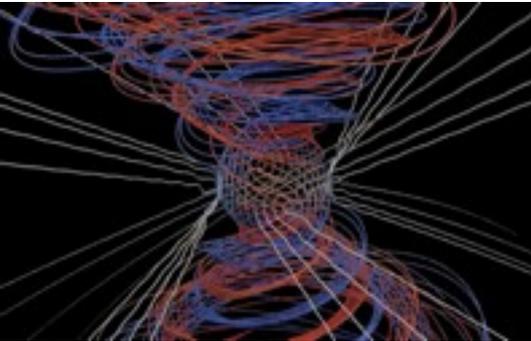
Mirror Surface
Thermal Fluctuations







Motivations for 3rd Gen Detectors



- 2nd Generation Detectors will have many detections, but likely very few high SNR events
- 3G design aims for 3x higher SNR over the whole band

- Tests of Fundamental Physics

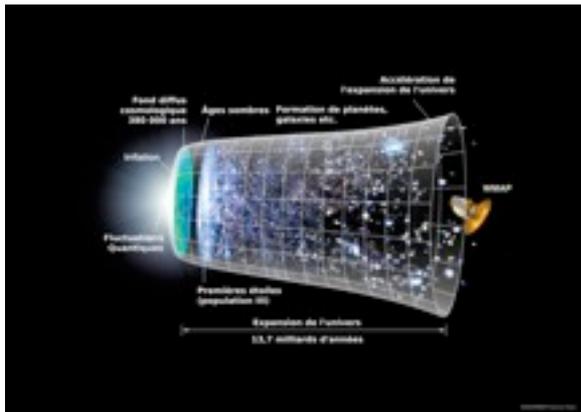
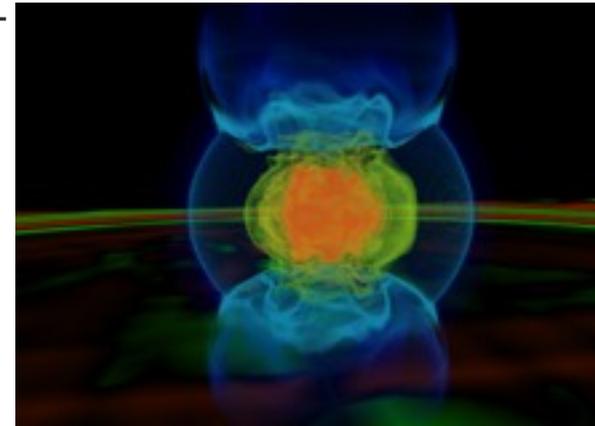
- » massive gravitons, scalar-tensor, vector-tensor, no hair theorem, higher dimensional theories

- Relativistic Astrophysics w/ EM

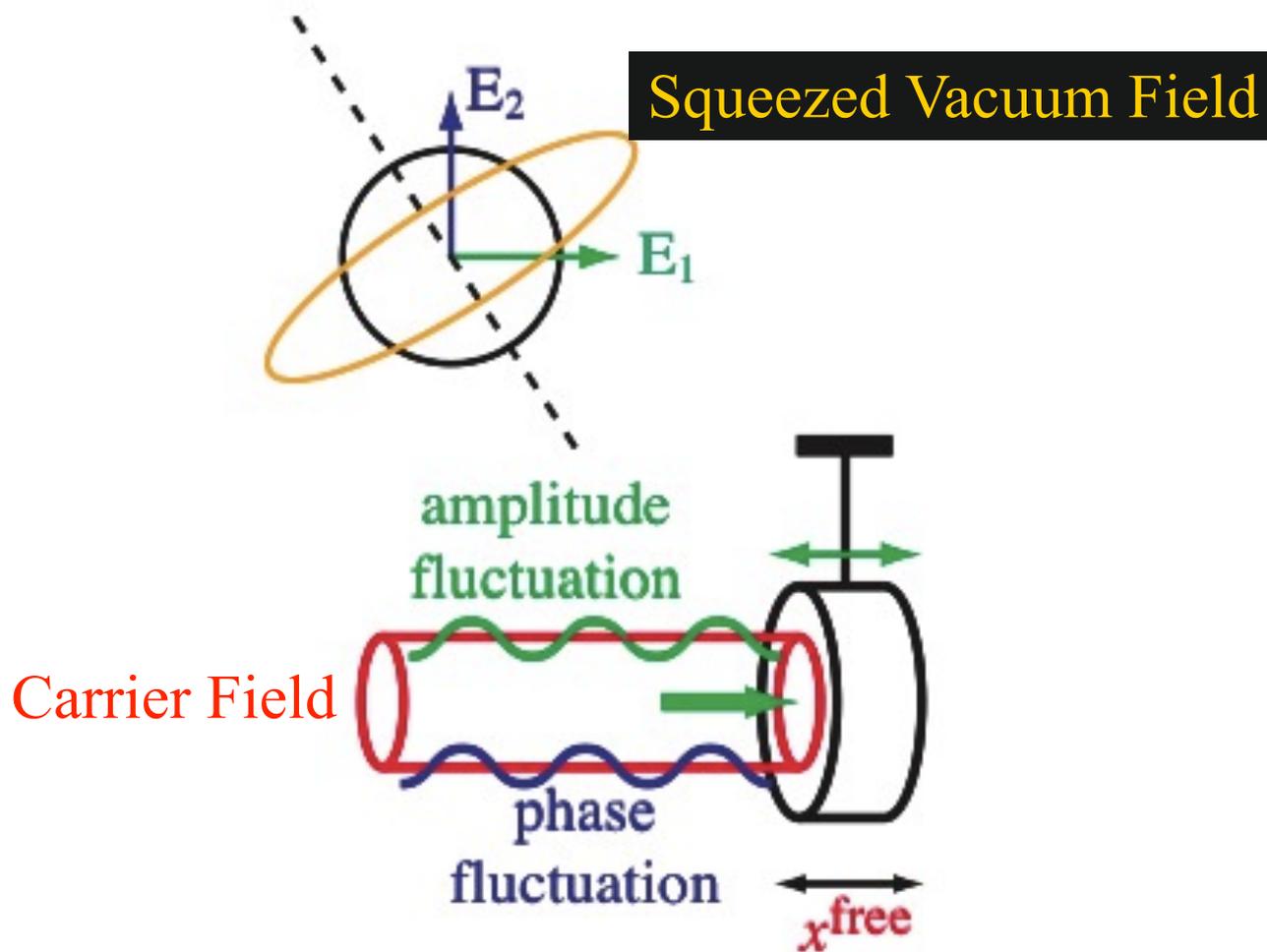
- » Extragalactic Supernovae, GRBs, Intermediate Mass BHs

- Cosmology

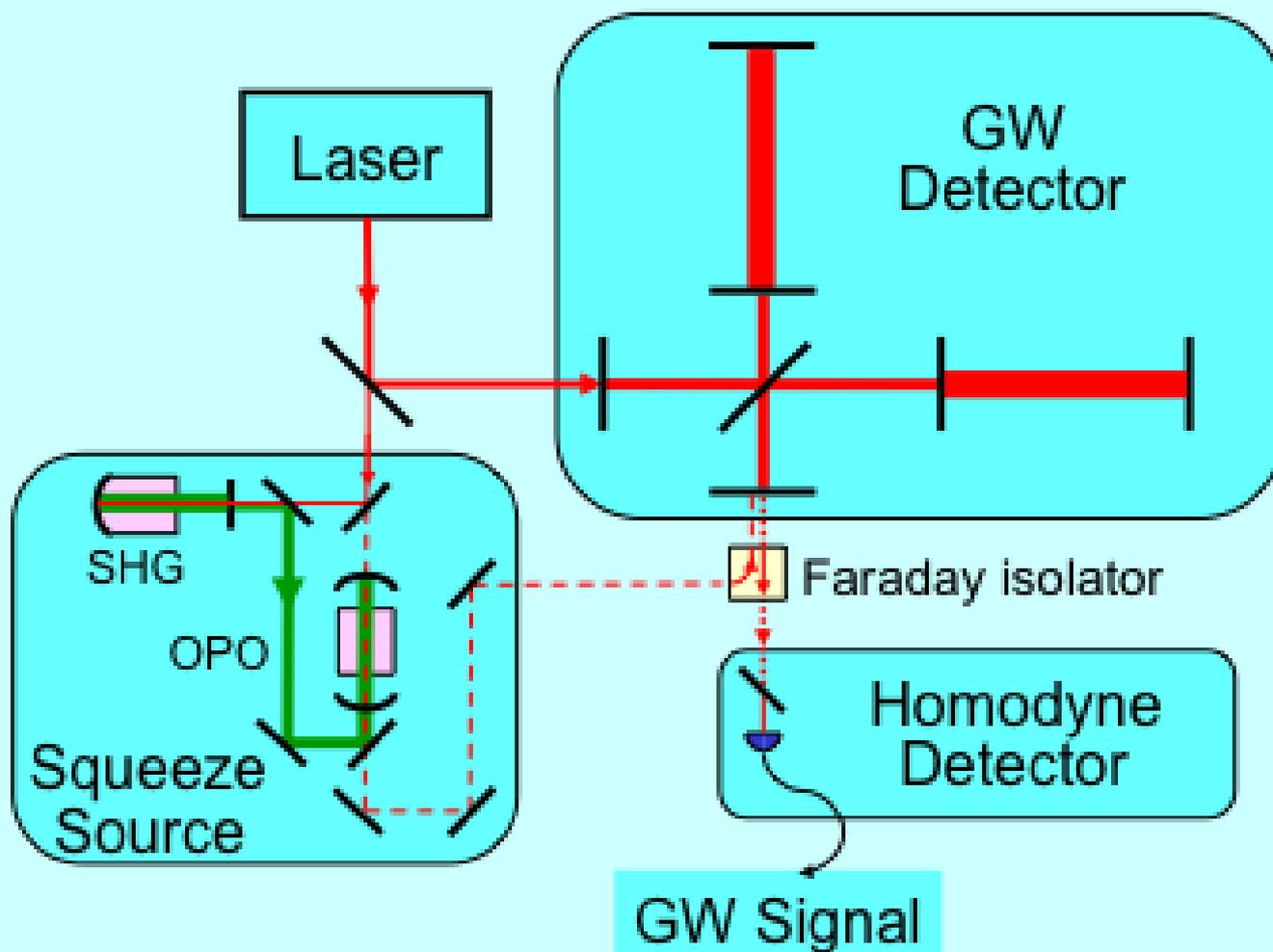
- » Standard GW ‘sirens’ for distance determination, fit to Concordance model (DM / DE densities)
- » GUT scale phase transitions, cosmic strings
- » The Unknown



Circumventing Usual Quantum Noise

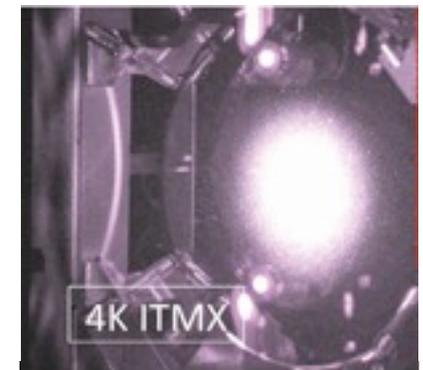
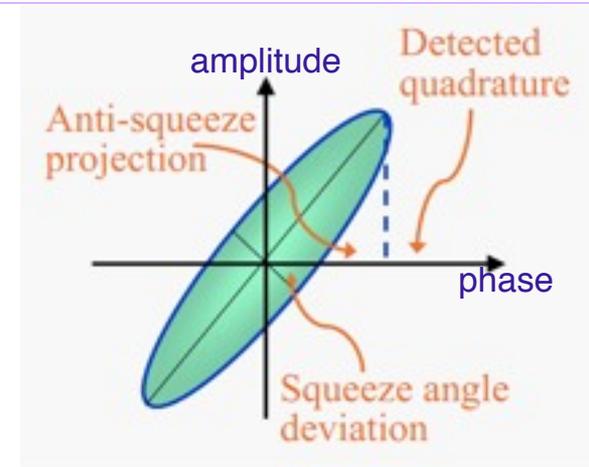


Squeezed Input Interferometer

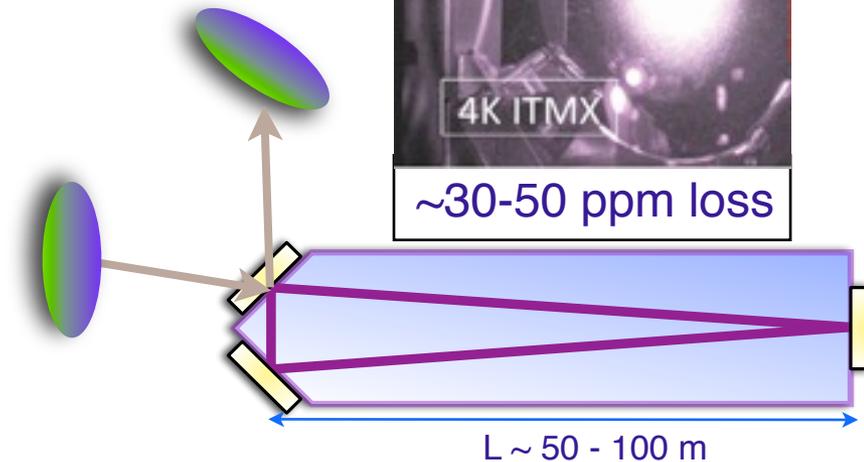


Quantum Noise Reduction

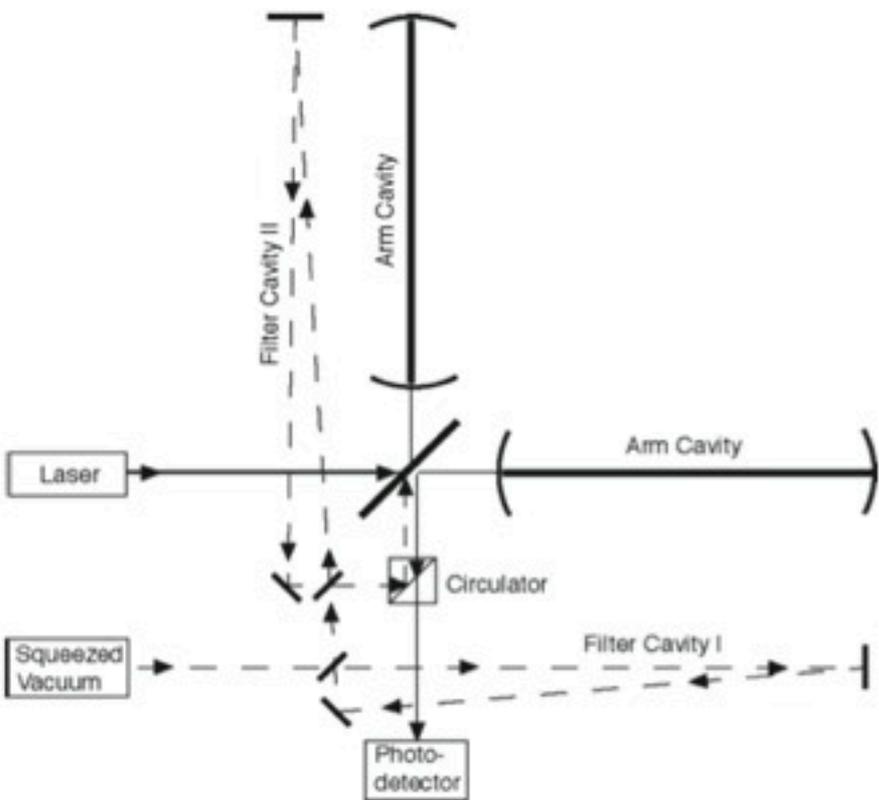
- Shot Noise limits at high frequency
- Quantum Radiation Pressure fluctuations limit at low frequencies
- Laser power 'knob' allows for a trade off; limited by interferometer thermal instability on the high power end
- **Squeezed Light Injection** can re-allocate the quantum noise (phase noise v. amplitude noise)
 - Demonstrated on IFOs at GEO600, LIGO Hanford
- **Frequency Dependent** Squeeze Angle
 - Long cavities act as optical phase shifters
 - Prototyping of 10-20m cavity at MIT
- **Needs:**
 - **Ultra-low loss optics (~10 ppm / bounce)**
 - 10 dB of squeezing *into the interferometer*
 - Low loss viewports, isolators, etc.



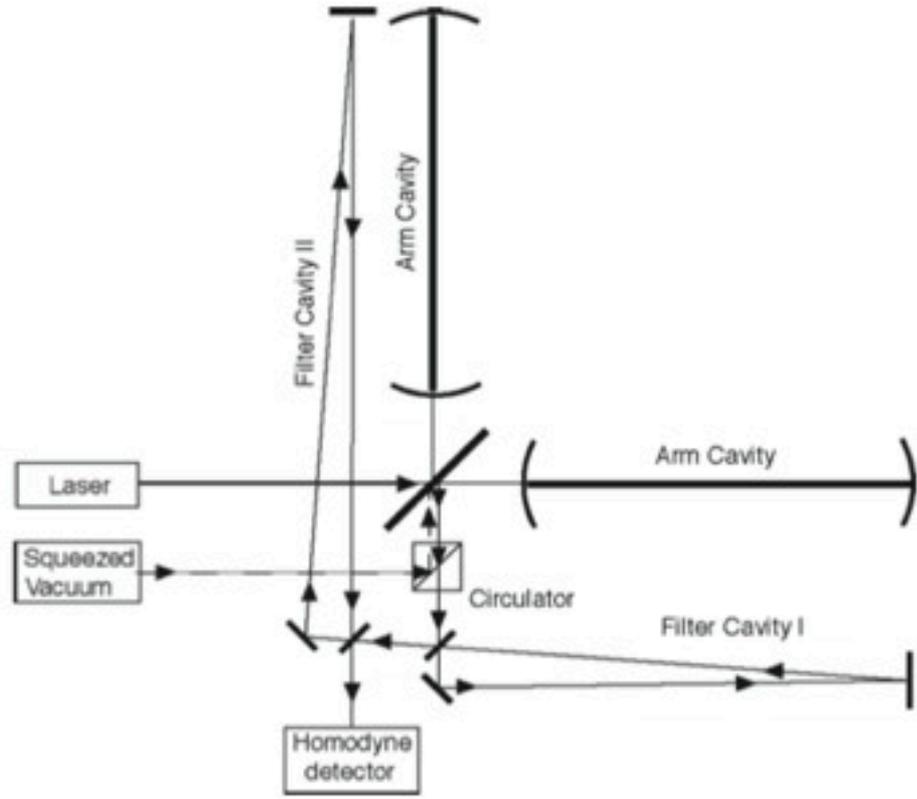
~30-50 ppm loss



Harms, et. al., PRD (2003)



Squeezed Input
 frequency dependent
 input squeezing quadrature



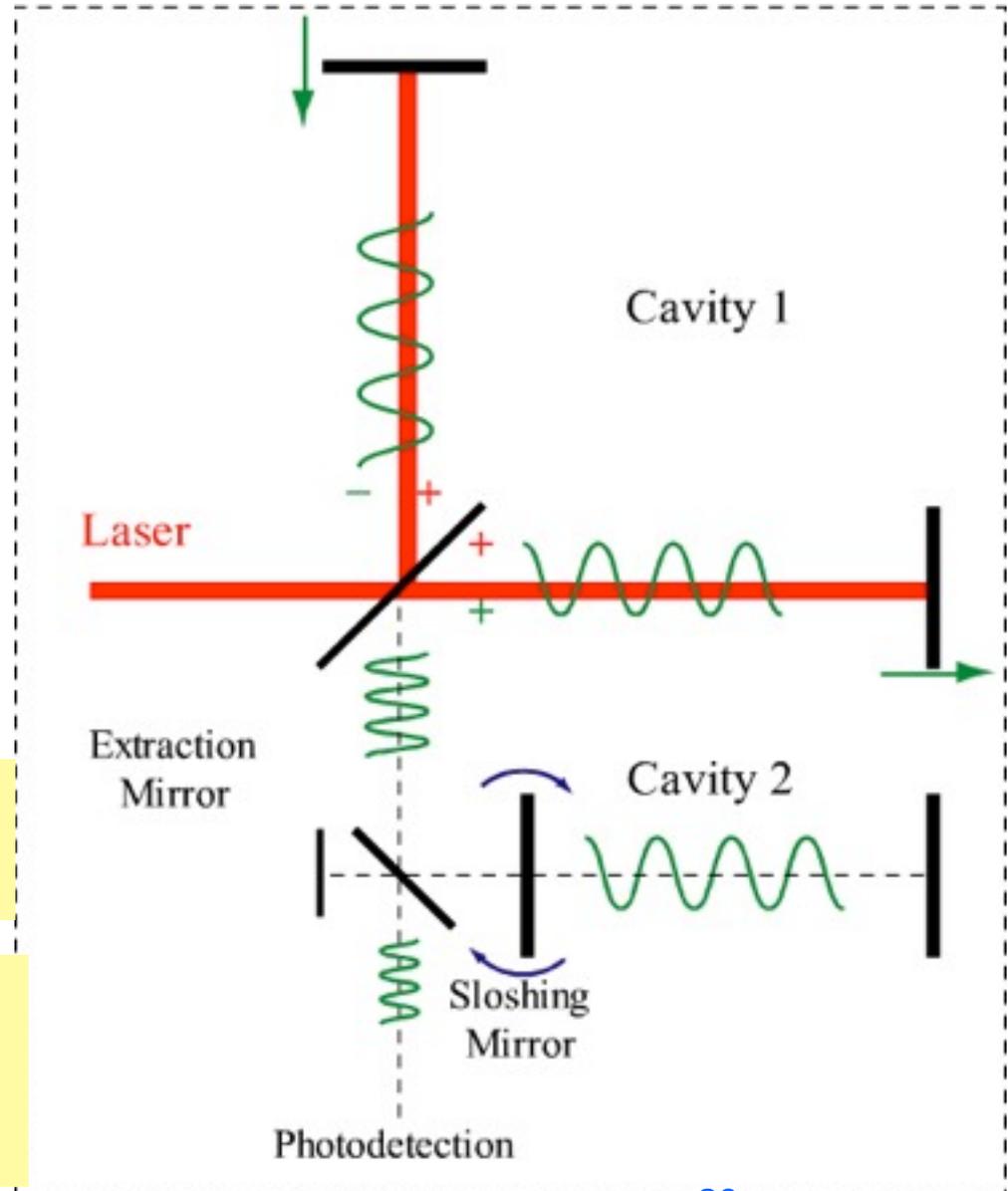
Variational Readout
 frequency dependent
 readout quadrature

QND via momentum

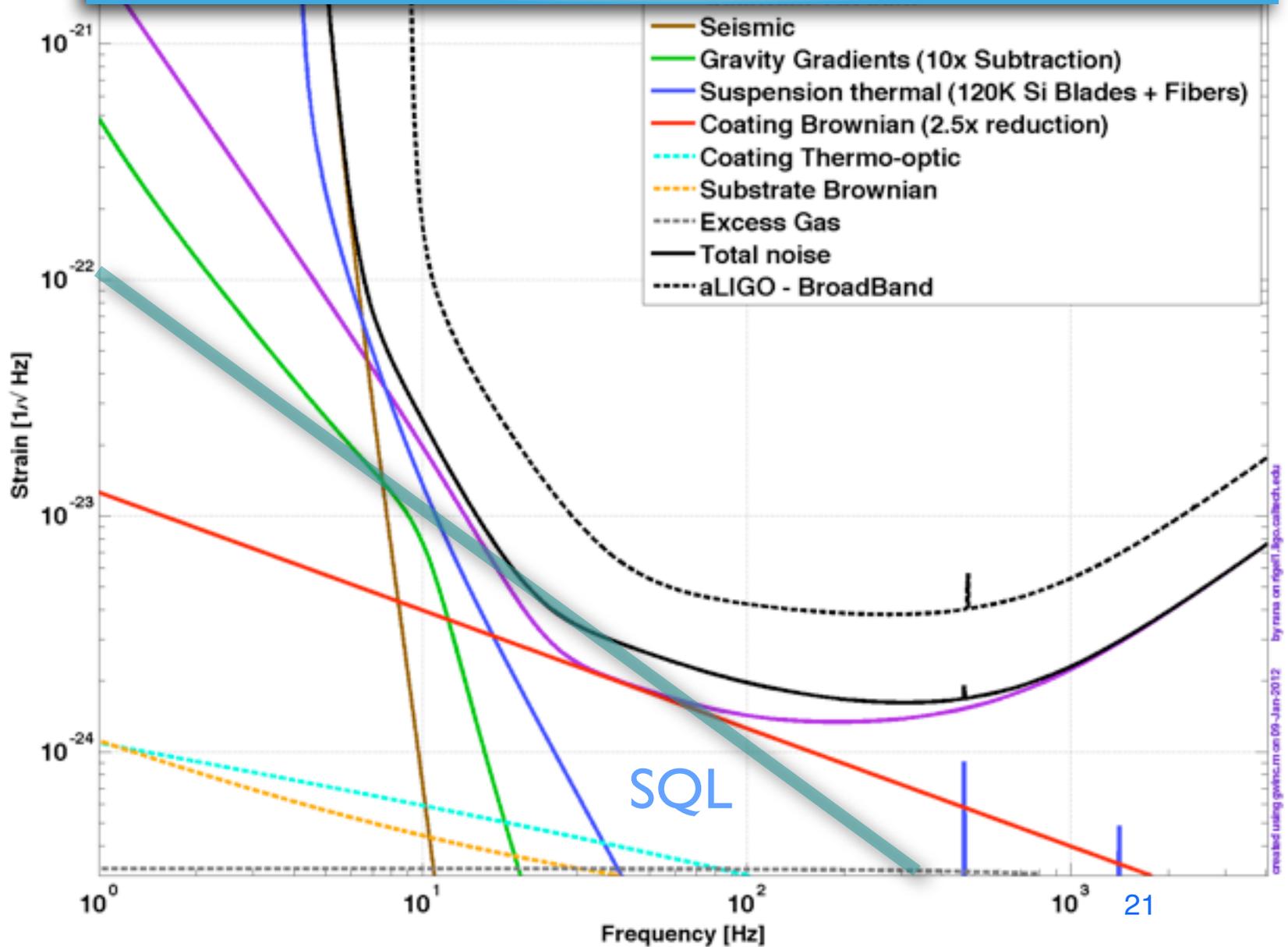
- Radiation pressure noise from dark port
- Some light experiences delay via the sloshing cavity
- Delay leads to phase flip for momentum kicks
- **Broadband Speedmeter**
 - req. low loss optics
 - req. very long cavities

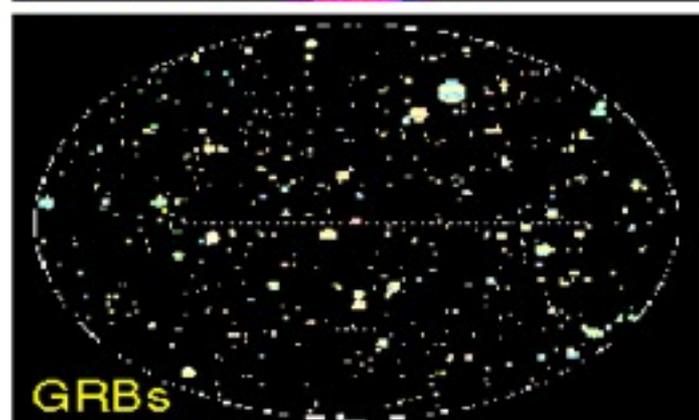
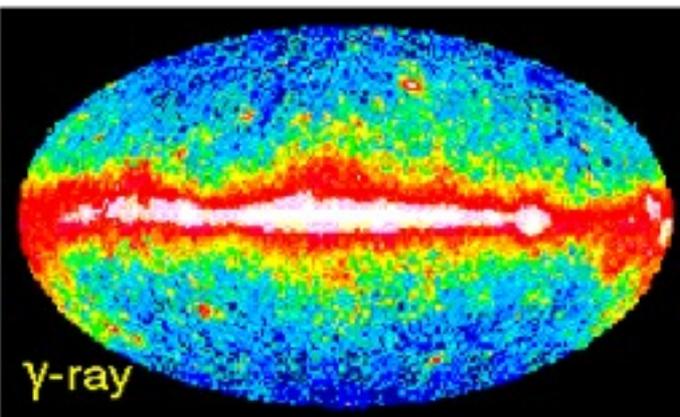
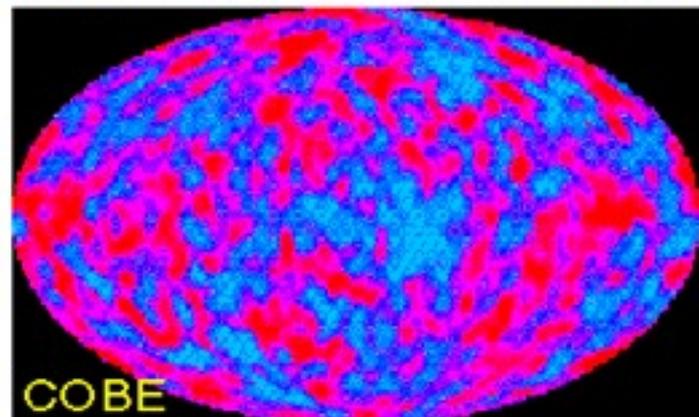
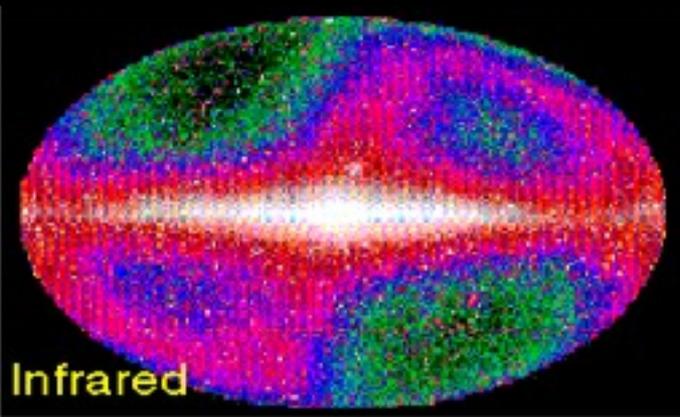
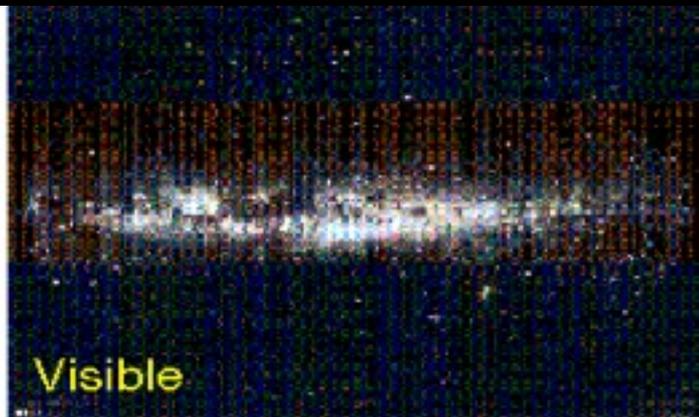
Momentum is a QND observable

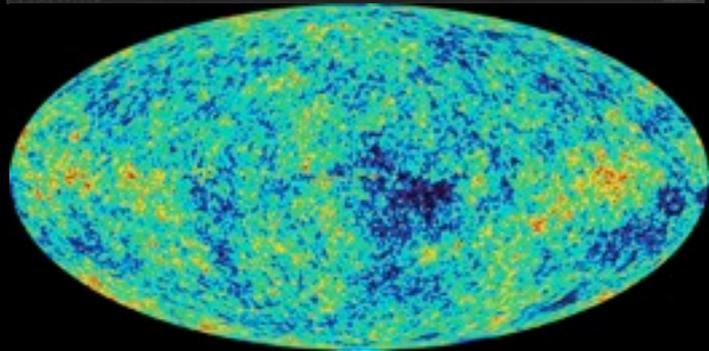
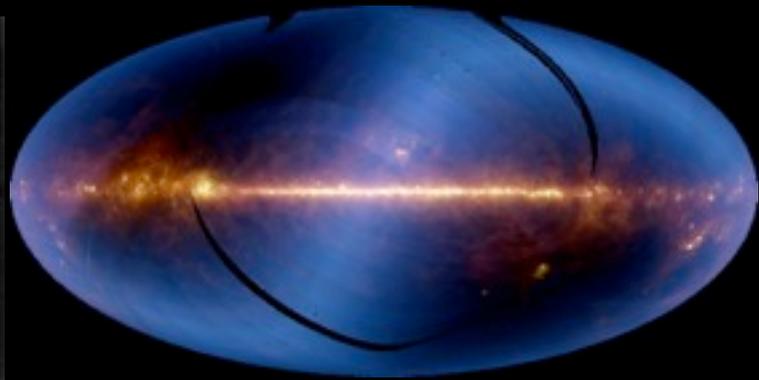
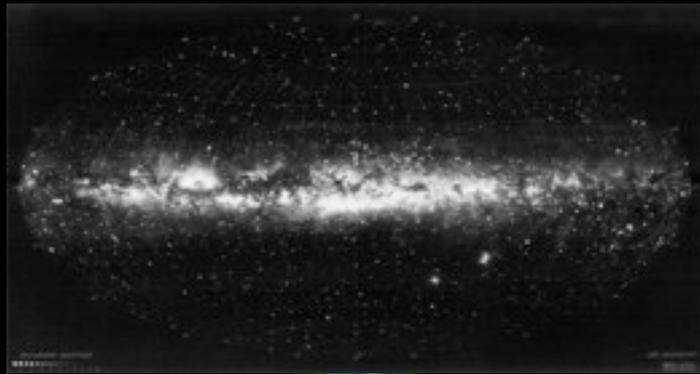
Observe momentum, perturb position. Position noise doesn't influence momentum.



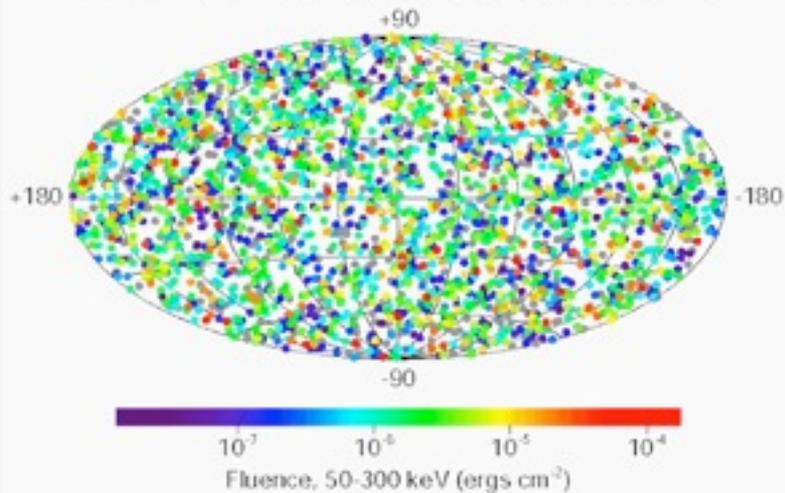
3rd Generation LIGO







2704 BATSE Gamma-Ray Bursts



SUMMARY

- 2nd Generation Interferometers ~ 2014
- 3rd Generation Interferometers ~ 2020
- Tests of NS physics, GR, discoveries of new phenomena
- Macroscopic Quantum Mechanics